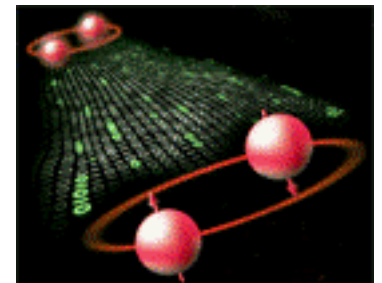


# Topological Quantum Phases and Light Spheres

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# Periodic Table of Topological Invariants: Application of Topology to Physics

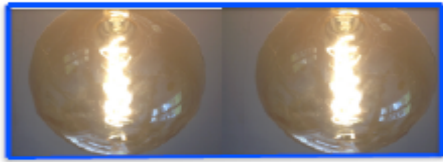
## Topological Insulators and Superconductors

Symmetry Class	Time reversal symmetry	Particle hole symmetry	Chiral symmetry
A	No	No	No
AIII	No	No	Yes
AI	Yes, $T^2 = 1$	No	No
BDI	Yes, $T^2 = 1$	Yes, $C^2 = 1$	Yes
D	No	Yes, $C^2 = 1$	No
DIII	Yes, $T^2 = -1$	Yes, $C^2 = 1$	Yes
AII	Yes, $T^2 = -1$	No	No
CII	Yes, $T^2 = -1$	Yes, $C^2 = -1$	Yes
C	No	Yes, $C^2 = -1$	No
CI	Yes, $T^2 = 1$	Yes, $C^2 = -1$	Yes

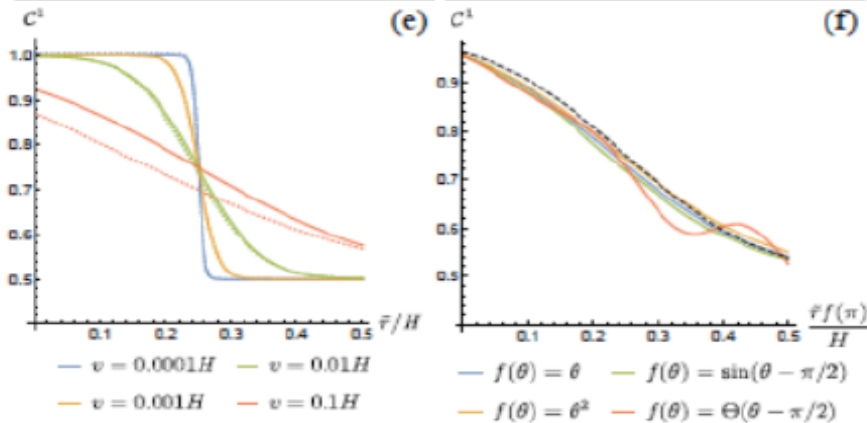
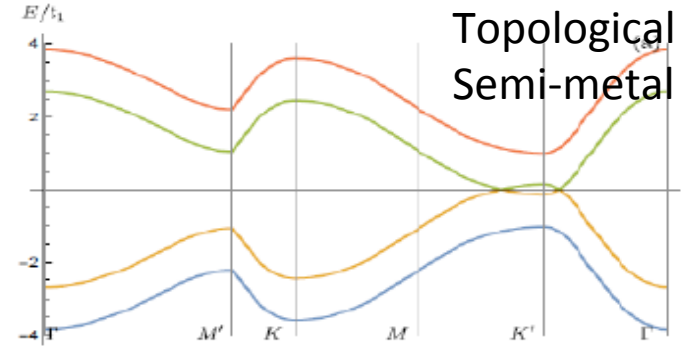
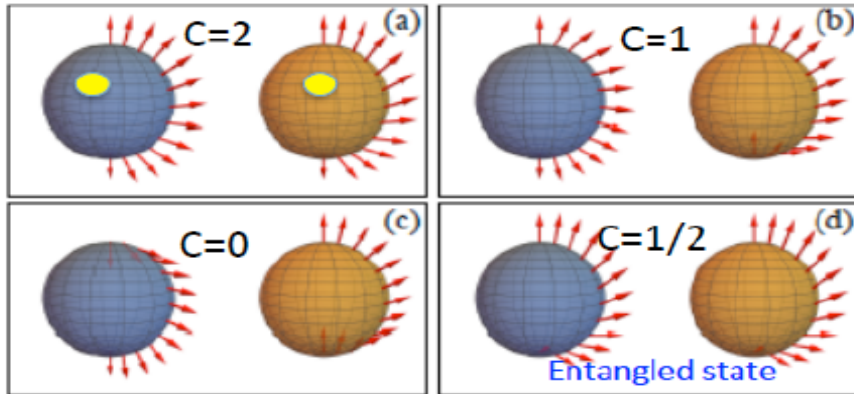
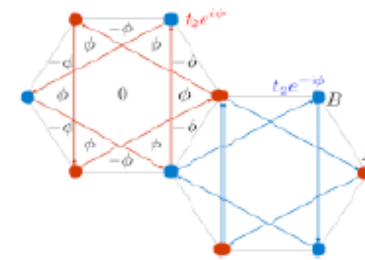
Topological states are characterized by a [topological invariant](#) linked to transport  
 Topology can also be achieved by applying a [radial magnetic field on a \(Bloch\) sphere](#)

Analogy to Gauss' law for electromagnetism  
 Realized with current technology, spin-1/2 in curved space





Spheres realizable  
in cQED mesoscopic  
and atomic systems



spheres	lattices
Spin 1/2	- 2 sublattices - Nambu basis
Radial Field on $S^2$	- Haldane model - P-wave SC - Resonating Bonds

Topological  
Semi-metal

Joel Hutchinson and Karyn Le Hur arXiv:2002.11823 and Communications Physics 1, 11 (2021)  
<https://www.nature.com/articles/s42005-021-00641-0>

Peng Cheng, Philipp W. Klein, Kirill Plekhanov, Klaus Sengstock, Monika Aidelsburger, Christoph Weitenberg, Karyn Le Hur, Phys. Rev. B (2019), application in bilayer systems

# New Objectives

<https://www.nature.com/articles/s42005-021-00641-0>

Circuit with more spheres: wire model in curved space

Analogy with coupled planes models and coupled wires, 3D

Quantum Hall Effect, Topological insulators and superconductors

<https://arxiv.org/abs/1910.04816>

<https://journals.aps.org/prresearch/abstract/10.1103/PhysRevResearch.2.022043>

- Interaction Effects, stochastic approach and Coulomb Forces

<https://arxiv.org/abs/2002.01742>

- New Geometry, Transport and Light-Matter Systems

<https://arxiv.org/abs/2106.15665>

- Time Protocols, Measures and Entanglement, codes

<https://arxiv.org/abs/1901.06489>

<https://arxiv.org/abs/1702.05135>

- Applications for Energy as Emitter of Light, quantum dynamo effect

<https://arxiv.org/abs/1611.05085>