

Topological Proximity Effect in Layer Systems

CPhT PhD Day 2018

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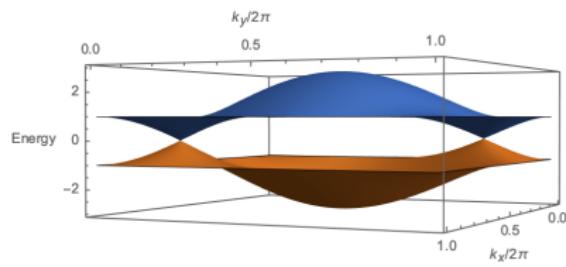
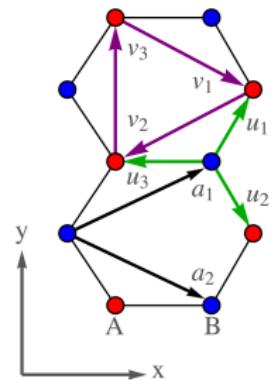


Haldane's graphene model

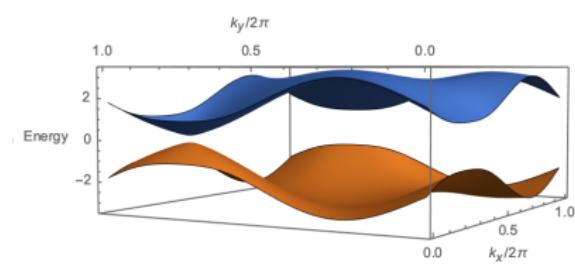
Haldane model

$$\mathcal{H}_0 = \sum_i (-1)^i M c_i^\dagger c_i - \sum_{\langle i,j \rangle} t_1 c_i^\dagger c_j - \sum_{\ll i,j \gg} t_2 e^{i\phi_{ij}} c_i^\dagger c_j$$

F. D. M. Haldane, Phys. Rev. Lett. 61, 2015 (1988)



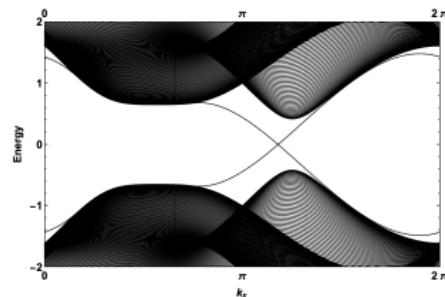
graphene



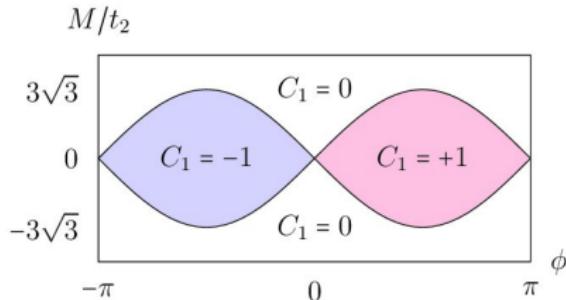
Haldane model

Haldane's graphene model

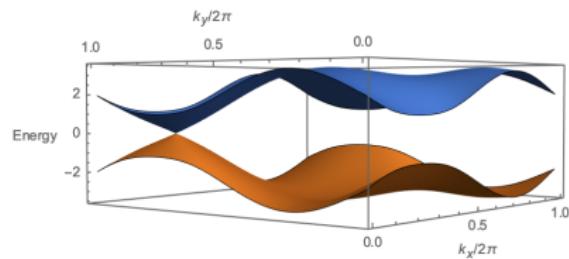
- bulk completely gapped for $M < 3\sqrt{3}t_2 \sin \phi$
- gap closing at $M = 3\sqrt{3}t_2 \sin \phi$
- Chern insulator: $C_1 = \pm 1$



Haldane model edge spectrum



Haldane model phase diagram



band spectrum at phase transition

Haldane-Graphene bilayer

Cheng, Klein (EP), Plekhanov (EP, Basel), Sengstock, Weitenberg (Hamburg), Le Hur (EP)

- consider two layer system:

$$H = H_h + H_g + H_r$$

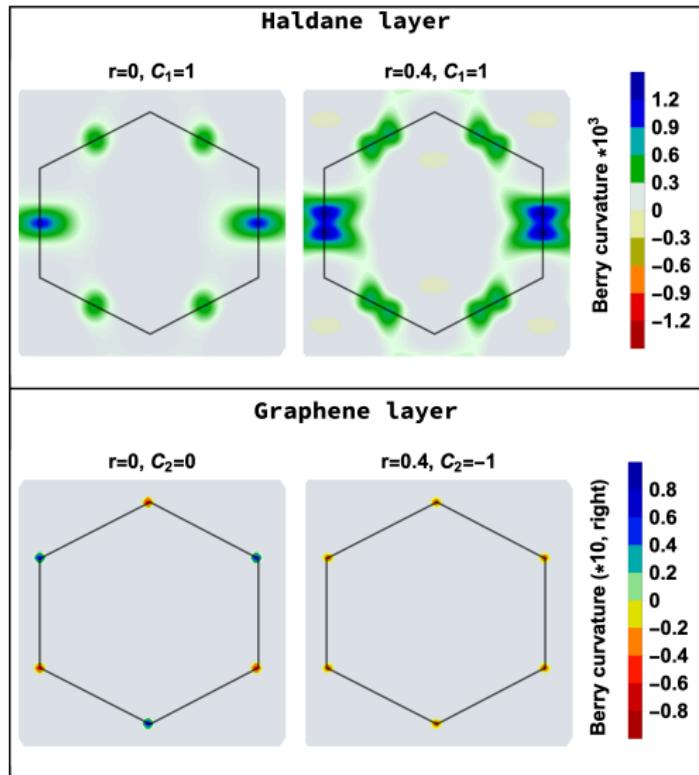
- graphene layer acquires non trivial topology, induced by Haldane layer

$$r = 0 : \quad C_i = (1, 0, 0, -1)$$

$$r \neq 0 : \quad C_i = (1, -1, 1, -1)$$

- note:

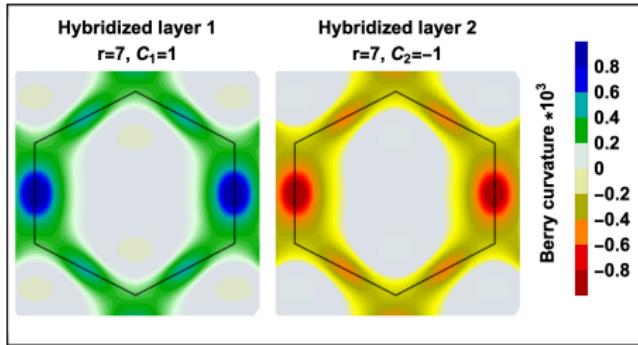
$$r \neq 0 : \quad C_1 + C_2 = 0$$



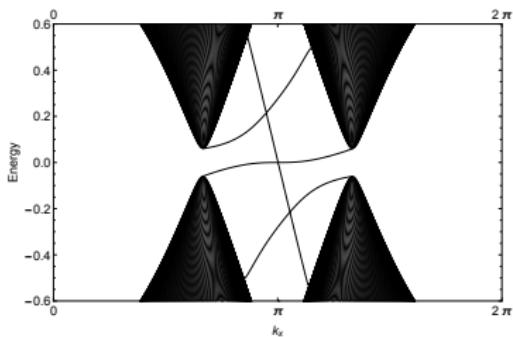
Haldane-Graphene bilayer

Cheng, Klein (EP), Plekhanov (EP, Basel), Sengstock, Weitenberg (Hamburg), Le Hur (EP)

- for large r , Berry curvature maps resemble each other
- suppress tunneling r at one edge
→ Kane-Mele like model but not \mathbb{Z}_2
→ counter-propagating but different velocities



Berry curvature at large r



suppressed r at one edge